

A New Model for Software Reliability Evaluation Based on NHPP with Imperfect Debugging

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Abstract — In new software products, the necessity of high reliability software development is increasingly important to all software developers and customers. Software reliability modeling based on Non Homogenous Poisson Process (NHPP) is one of the successful methods in predicting software reliability. One of the most important assumptions in modeling software reliability is imperfect phenomenon which describes the probability of introducing new faults to the software during debugging process. In this paper a new imperfect model is proposed by considering complexity and dependency between faults. Estimating the model parameters has been done by using failure data sets of four real software projects through MATLAB software. Comparison of the proposed model is done with two existing models using various criteria. The results show that the proposed model better fits the real data and then providing more accurate information about the software quality.

Keywords — Software Reliability, Non Homogenous Poisson Process, simple and complex faults, dependency, time delay, imperfect debugging

1. INTRODUCTION

An important approach in evaluating software quality and performance is to determine the software reliability. Software reliability defined as the probability of error free software operation in a specified environment for a specified time (Yamada, 2014). In the last three decades various software reliability growth models (SRGMs)¹ have been developed. Most of the SRGMs based on NHPP present the reliability diagram as concave or S-shaped curve (Goel, 1985; Pham, 2006; Kapur, et al., 2011; Lai, et al., 2012). If the reliability is uniformly growth, concave models are used otherwise it would be S-shaped. In 1985 Goel and Okumoto proposed a concave model which assumed that total faults in the software are independent and probability of detecting faults in a unit of time is constant (Goel, 1985). They also assumed detected faults are immediately removed and no new faults are introduced during debugging (perfect debugging). In an S-shaped model detected faults are

immediately removed and perfect debugging is used but fault detection rate is time dependent (Yamada, et al., 1983; Yamada, et al., 1984; Yamada, et al., 1985). In lots of recent researches imperfect debugging is considered in modeling, which shows the probability of introducing new faults to the software during fault correction and removal (Yamada, et al., 1992; Pham, 2006; Pham, 2007; Gagarwal, et al., 2011; Gupta, et al., 2011).

In some of developed models detected faults are categorized according to their dependency or complexity. Ohba proposed the idea of fault dependency in 1984 by assuming that independent faults can be removed immediately after they are detected but dependent faults cannot be removed until their leading faults are eliminated (Ohba, 1984). Kapour and Younes in 1995 affected fault dependency into G-O model (Kapur, et al., 1995). They noticed that time delay effect factor between detecting and removing dependent faults is negligible. In studies by Hung and Lin dependent and independent faults are modeled based on NHPP with some various times dependent delay functions (Huang, et al., 2004; Huang, et al., 2006).

Karee and his colleagues proposed an S-shaped model with fault complexity by categorizing faults as simple and hard. In their model simple faults can be removed immediately but they affected two steps of observing and removing to eliminate hard faults (Kareer, et al., 1990). Kapur In 1999 developed a model by considering software testing as a three step process, including observing, isolating and removing faults. Based on this assumption, he proposed a model with three types of faults categorized based on their complexity. In which simple faults can be removed immediately after they are detected, hard faults are those that need a time delay factor between observing and isolating the fault and complex faults need a time delay effect factor between observing, isolating and removing the fault (Kapur, et al., 1999).

In this paper an imperfect model based on both complexity and dependency of faults is developed. Software faults are categorized in terms of their complexity into two types of simple and complex, and complex faults are classified into independent and dependent. Then, three different types of faults are

¹Software Reliability Growth Model

proposed and for each type, an appropriate modeling is presented based on some assumptions.

In software reliability modeling there are unknown parameters that can be determined by Maximum Likelihood Estimation (MLE) or least squared estimation methods (Zacks, 1992; Pham, 2006). The unknown parameters of the proposed model are determined by using four real software fault data sets by MLE. Then some of statistical criteria are used to compare the goodness of fit of the new model and two basic models. The estimated time to stop testing for software is evaluated by the proposed model.

The remainder of paper is as follows: In Section 2, a generic NHPP software reliability model is explained. Section 3 is dedicated to one application of software reliability estimation, estimating time to stop software testing. In Section 4, the parameters, assumptions and our modeling is described in details. The next two sections, 5 and 6 are specified to model estimation, and model validation respectively. The paper is concluded in Section 7.

2. SOFTWARE RELIABILITY MODELING BASED ON NHPP

The basic assumption in NHPP modeling is that the failure process is described by the NHPP.

Most of software reliability growth models follow the general assumptions regarding the fault detection process which can be considered as follows.

- Detecting / removing faults are modeled by NHPP.
- All faults are independent from each other and they are equally recognizable.
- The number of faults detected at any time is proper with the number of remaining faults in the software.
- Each time a failure occurs an error that led to it is immediately and completely removed and no new errors introduced in the meantime (perfect debugging).

Assume that $N(t)$ is the number of detected errors (failures observed) at time t and $m(t)$ is the mean number of detected faults until time t , then its Min Value Function (MVF) is:

$$Pr N(t) = n = \frac{m(t)^n}{n!} e^{-m(t)} \quad n = 0, 1, 2, \dots \quad (1)$$

Where $m(t) = \int_0^t \lambda(s) ds$ and $\lambda(t)$ is failure intensity

function (number of failures per unit of time).

$$\frac{dm(t)}{dt} = \lambda(t) \quad (2)$$

Therefore, the overall reliability model based on NHPP is obtained by solving the following differential equation with the initial condition $m(0) = 0$:

$$\lambda(t) = \frac{dm(t)}{dt} = b(t) \cdot (a - m(t)) \quad (3)$$

In which, "a" represents the total number of initial faults in the software before testing. Expression $[a - m(t)]$ shows

the mean number of remaining faults in the software at time t , and $b(t)$ is fault detection rate.

General solution for the differential equation 3 is as follows:

$$m(t) = e^{-\beta t} [C + \int_0^t ab(t) e^{\beta t} dt] \quad (4)$$

In which:

$$\beta(t) = \int b(t) dt$$

And C is the constant of integration.

Finally the software reliability is achieved through the following formula:

$$R(t) = e^{-\int_0^t \lambda(s) ds} \quad (5)$$

Table1 [3] shows details of two basic models for software reliability, Goel - Okumoto exponential model and delayed S-shaped model.

Table 1. Details of exponential and delayed s-shape models

Model name	Mean value function $m(t)$	Fault detection rate $b(t)$
Exponential	$a(1 - e^{-bt})$	b
Delayed S-shape	$a(1 - \frac{1}{1+bt})e^{-bt}$	$b(t) = \frac{b^2 t}{1+bt}$

3. ESTIMATING TIME TO STOP SOFTWARE TESTING

Software testing is a costly process, so it's necessary to terminate it in a suitable time. One of the applications of estimating software reliability is to determine the appropriate time to terminate software testing. If the software reached to an acceptable level of reliability at the specified time, then decision to terminating the test can be taken. To achieve this goal, the conditional reliability function, $R(x|t)$ is used. This function assumes that the last failure has occurred at time t and no new failure happens at time interval $t, t+x$. Therefore (Pham, 2006):

$$R(x|t) = Pr N(t+x) - N(t) = 0 = e^{-m(t+x) - m(t)} \quad (6)$$

4. THE PROPOSED MODEL

In this section, first the model parameters and assumptions are presented and then, according to the provided assumptions, the modeling is carried out.

4.1. PARAMETERS OF THE PROPOSED MODEL

a : total number of initial faults in the software.

a_1, a_2, a_3 : total number of initial simple, independent complex, dependent complex faults.

b_1, b_2, b_3 : fault detection rate for Simple, independent complex, dependent complex faults

$\alpha_1, \alpha_2, \alpha_3$: fault introduction rate for simple, independent complex, dependent complex faults.

P : proportion of simple and complex errors in software

q: proportion of independent complex and dependent complex.

$\varphi_1 t$: time lag for complex independent faults.

$\varphi_2 t$: time lag for complex dependent faults.

$m t$: mean value function for total software faults.

$m_1 t$: mean value function for simple faults.

$m_2 t - \varphi_1 t$: mean value function for independent complex faults.

$m_3 t - \varphi_2 t$: mean value function for the dependent complex faults.

4.2. ASSUMPTIONS OF THE PROPOSED MODEL

Our proposed model assumptions are as follows:

- i. Detecting / removing faults is modelled by NHPP.
- ii. Software faults are divided into simple and complex faults. This division was done by considering the amount of effort needed to remove them.
- iii. Simple faults can be corrected and deleted immediately after detection.
- iv. Complex faults may need more effort to be removed. This kind of fault is considered in dependent and independent.
- v. Independent complex faults need more times than simple faults to be removed. Therefore the time delay factor $\varphi_1 t$ is affected to show the amount of efforts is needed for this type of faults.
- vi. Dependent complex faults arise due to the presence of an independent complex fault. This kind of fault cannot be removed unless its leading fault is eliminated. According to the effort required in removing this type of fault, time delay factor is not negligible, therefore the latency $\varphi_2 t$ will be affected
- vii. During the debugging process, introducing new faults is possible to show the imperfect phenomenon.

4.3. MODELING

The total number of detected faults during the time (0, t) is equal to:

$$m t = m_1 t + m_2 t - \varphi_1 t + m_3 t - \varphi_2 t \quad (7)$$

Let a be the total number of initial faults before testing and a_1, a_2, a_3 describe total number of initial simple, independent complex and dependent complex faults respectively. So we have:

$$a_1 = pa \quad a_2 = 1 - p \quad qa \quad a_3 = 1 - p \quad 1 - qa$$

Detection and removal process of simple faults follows the general reliability modeling (Equation 3) with constant b_1 fault detection rate.

Of course time lag to remove faults is negligible and imperfect debugging is affected by α_1 new faults introduced to software during debugging as shown in equation (8):

$$\frac{dm_1 t}{dt} = b_1 a_1 + \alpha_1 m_1 t - m_1 t \quad (8)$$

By solving the differential equation (8), the mean value function of the detected faults is created as follows :

$$m_1 t = \frac{a_1}{1 - \alpha_1} 1 - e^{-b_1 t 1 - \alpha_1} = \frac{pa}{1 - \alpha_1} 1 - e^{-b_1 t 1 - \alpha_1} \quad (9)$$

Software debugging team requires more time to discover the causes of complex faults to remove them. For this type of faults general model of reliability can be used, however it is necessary to affect time delay factor and imperfect debugging in removal process.

Assuming that the mean value function of the independent complex faults is proportional to the remaining number of independent complex faults and α_2 new faults introduced to the system, so:

$$\frac{dm_2 t}{dt} = b_2 a_2 + \alpha_2 m_2 t - m_2 t \quad (10)$$

By solving the differential equation (10), in initial condition $m_2 0 = 0$ will have:

$$m_2 t = \frac{a_2}{1 - \alpha_2} 1 - e^{-b_2 t 1 - \alpha_2} = \frac{1 - p \quad qa}{1 - \alpha_2} 1 - e^{-b_2 t 1 - \alpha_2} \quad (11)$$

Time delay factor in debugging of independent complex faults is considered as ascending function $\varphi_1 t$. Thus the finalequation (12) is obtained:

$$\varphi_1 t = \left(\frac{\ln 1 + b_2 t}{b_2} \right)$$

$$m_2 t - \varphi_1 t = \frac{1 - p \quad qa}{1 - \alpha_2} \left[1 - 1 + b_2 t^{1 - \alpha_2} e^{-b_2 t 1 - \alpha_2} \right] \quad (12)$$

Based on assumption v, the general modeling of reliability is not directly applicable on removing dependent complex faults.

The mean value of dependent complex faults is proportional to the number of remaining dependent complex faults, the mean value of independent complex faults and α_3 new introduced faults to the system. Also, time delay factor $\varphi_2 t$ and imperfect debugging are affected to remove this kind of faults. So the differential equation for modeling these faults is as follows:

$$\frac{dm_3 t}{dt} = b_3 a_3 + \alpha_3 m_3 t - m_3 t - \frac{m_2 t - \varphi_1 t}{a_2 + a_3} \quad (13)$$

By solving equation (13), we obtain :

$$m_3 t = \frac{a_3}{1 - \alpha_3} \times (14)$$

$$\left[1 - \exp \left(\frac{-a_3 b_3^2 1 - \alpha_3}{a_2 + a_3 1 - \alpha_2} \times \int_0^t \frac{s}{b_3 s + 1} (1 - 1 + b_2 s^{1 - \alpha_2} e^{-b_2 s 1 - \alpha_2}) ds \right) \right]$$

Considering the time required for debugging and removing complex dependent faults, time delay factor

$\varphi_2 t$ should be affected in Equation (14) for the final equation of complex dependent faults. So we have:

$$\varphi_2 t = \left(\frac{\ln(1 + b_3 t)}{b_3} \right)$$

$$m_3 t - \varphi_2 t = \quad (15)$$

$$\frac{a_3}{1 - a_3} \left[1 - \exp \left(\frac{-a_2 b_3^2 (1 - a_3)}{a_2 + a_3 (1 - a_2)} \times \int_0^{t - \varphi_2 t} \frac{s}{b_3 s + 1} (1 - 1 + b_2 s)^{1 - a_2} e^{-b_2 s (1 - a_2)} ds \right) \right]$$

According to equation (7), the mean value function of total software's faults is obtained by calculating all three mean value functions.

5. MODEL ESTIMATION

The proposed model is tested on four real software failure data sets, real-time command and control system (Ohba, 1984a), IBM (Musa, et al., 1987), OCS (Pham, et al., 2003) and Misra (Misra, 1983) and its parameters are estimated by Matlab2012 software. Table (2) presents estimated parameters for the proposed model, exponential model and delayed S-shaped model.

Table2.Parameter estimation based on failure datasets

Model name	Misra	OCS	IBM	Real time
New model	$\hat{a} = 378$	$\hat{a} = 380$	$\hat{a} = 71$	$\hat{a} = 150$
	$\hat{b}_1 = 0 / 69$	$\hat{b}_1 = 0 / 18$	$\hat{b}_1 = 0 / 03$	$\hat{b}_1 = 0 / 5$
	$\hat{b}_2 = 0 / 16$	$\hat{b}_2 = 0 / 19$	$\hat{b}_2 = 0 / 09$	$\hat{b}_2 = 0 / 13$
	$\hat{b}_3 = 0 / 09$	$\hat{b}_3 = 0 / 0001$	$\hat{b}_3 = 0 / 99$	$\hat{b}_3 = 0 / 0001$
	$\hat{s} = 0 / 06$	$\hat{s} = 0 / 17$	$\hat{s} = 0 / 43$	$\hat{s} = 0 / 42$
		$\hat{q} = 0 / 34$	$\hat{q} = 0 / 56$	$\hat{q} = 0 / 94$
		$\hat{\alpha}_1 = 0 / 0001$	$\hat{\alpha}_1 = 0 / 0001$	$\hat{\alpha}_1 = 0 / 03$
	$\hat{q} = 0 / 21$	$\hat{\alpha}_2 = 0 / 0001$	$\hat{\alpha}_2 = 0 / 001$	$\hat{\alpha}_2 = 0 / 0001$
	$\hat{\alpha}_1 = 0 / 06$	$\hat{\alpha}_3 = 0 / 001$	$\hat{\alpha}_3 = 0 / 001$	$\hat{\alpha}_3 = 0 / 85$
		$\hat{\alpha}_2 = 0 / 54$		
	$\hat{\alpha}_3 = 0 / 99$			
G-O model	$\hat{a} = 922$	$\hat{a} = 242$	$\hat{a} = 400$	$\hat{a} = 142$
	$\hat{b} = 0 / 007$	$\hat{b} = 0 / 06$	$\hat{b} = 0 / 005$	$\hat{b} = 0 / 12$
Delayed S-shaped model	$\hat{a} = 285$	$\hat{a} = 153$	$\hat{a} = 71$	$\hat{a} = 136$
	$\hat{b} = 0 / 08$	$\hat{b} = 0 / 31$	$\hat{b} = 0 / 1$	$\hat{b} = 0 / 28$

Now using obtained parameters, mean value function and software reliability can be estimated in a time interval $t, t + 0.1$. Thus, the time termination of software testing is specified. Table (3) presents the information of software testing process obtained by using proposed model on real-time command and control system from

time 17 to 25 to estimate the software testing time termination.

Table3.Obtained information after each test of real-time command and control system to determine the terminating time of testing process using proposed model

Testing time (t)	Total number of estimated initial faults (\hat{a})	Value of Estimated Mean value function ($\hat{m}(t)$)	$\hat{R}(./1 t)$
17	134 / 218	122 / 178	0 / 703
18	195 / 860	126 / 691	0 / 669
19	249 / 163	128 / 040	0 / 729
20	329 / 759	128 / 998	0 / 879
21	132 / 299	131 / 292	0 / 773
22	189 / 805	131 / 995	0 / 836
23	252 / 901	134 / 001	0 / 843
24	263 / 681	134 / 997	0 / 864
25	149 / 949	135 / 999	0 / 881

6. MODEL VALIDATION

To show the validation of the proposed model assumptions, we compare it with exponential model and delayed S-shaped model which are considered as basic models in predicting software reliability, based on NHPP. Figures (1) to (4) shows the proposed model's goodness of fit compared with the exponential model and delay S-shaped model on all four data sets mentioned in the last section.

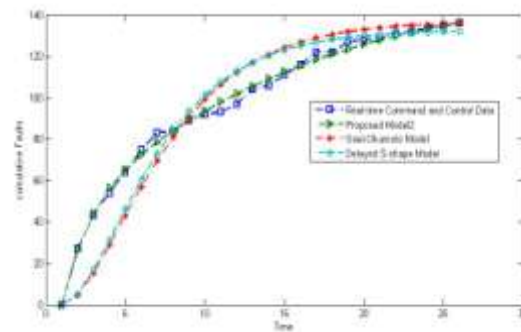


Figure1.proposed model's goodness of fit compared with, Exponential model and delay S- shaped model on real time command and control dataset

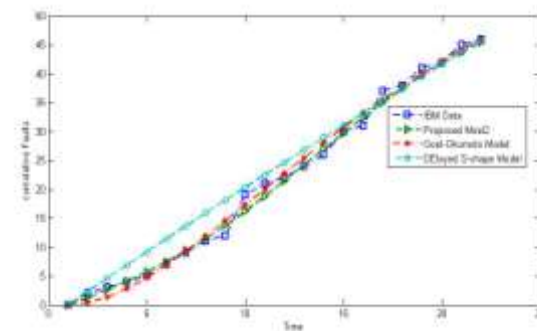


Figure2.proposed model's goodness of fit compared with, exponential model and delay S- shaped model on IBM dataset

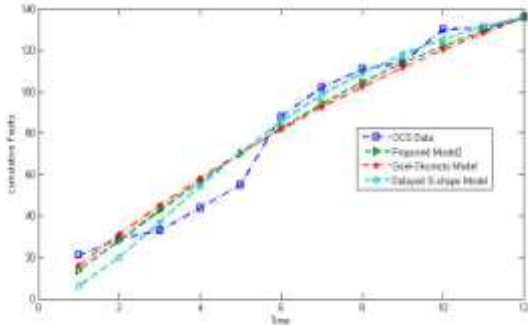


Figure 3. proposed model's goodness of fit compared with, Exponential model and delay S- shaped model on OCS dataset

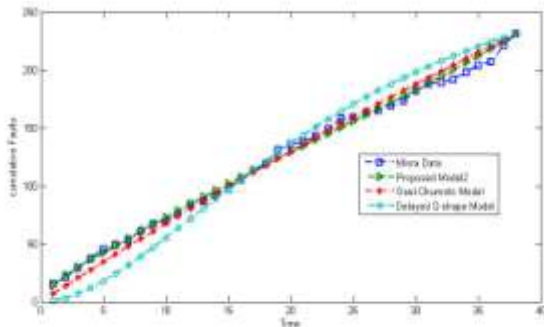


Figure 4. proposed model's goodness of fit compared with, Exponential model and delay S- shaped model on Misra dataset

It can be seen from figures, the proposed model is properly consistent on data sets.

For accurate model comparison, other criteria can be used. Three common ones are PRR¹ (Pham, et al., 2003), SSE² (Pham, 2006) and MSE³ (Pham, 2006), which can be expressed as follows:

$$PRR = \sum_{i=1}^n \left(\frac{m(t_i) - y_i}{m(t_i)} \right)^2$$

$$SSE = \sum_{i=1}^n (y_i - m(t_i))^2$$

$$MSE = \sum_{i=1}^n \frac{(m(t_i) - y_i)^2}{n}$$

"y" is total number of faults observed at time "t" according to real dataset and "m(t)" is estimated cumulative number of faults at time "t" and "n" is the number of observations.

In model comparison, smaller values for each of three criteria on the same dataset, represents more appropriate model.

Table (4) shows the obtained values of criteria for proposed model, exponential model and delayed S-shaped model on all four datasets.

Table3. values of criteria for proposed model, exponential model and delayed S-shaped model

Model name	Misra data set	OCS data set	IBM data set	Real-time Command and Control data set
New Model	<i>AIC</i> = 205 / 22 <i>PRR</i> = 0 / 05 <i>SSE</i> = 707 / 95 <i>MSE</i> = 18 / 63	<i>AIC</i> = 128 / 84 <i>PRR</i> = 0 / 46 <i>SSE</i> = 739 / 04 <i>MSE</i> = 19 / 44	<i>AIC</i> = 82 / 66 <i>PRR</i> = 0 / 49 <i>SSE</i> = 29 / 76 <i>MSE</i> = 1 / 41	<i>AIC</i> = 117 / 04 <i>PRR</i> = 0 / 01 <i>SSE</i> = 130 / 15 <i>MSE</i> = 5 / 20
G-O Model	<i>AIC</i> = 200 / 75 <i>PRR</i> = 2 / 06 <i>SSE</i> = 1 / 6571e + 03 <i>MSE</i> = 43 / 60	<i>AIC</i> = 117 / 07 <i>PRR</i> = 0 / 30 <i>SSE</i> = 921 / 88 <i>MSE</i> = 76 / 82	<i>AIC</i> = 77 / 71 <i>PRR</i> = 1 / 04 <i>SSE</i> = 170 / 82 <i>MSE</i> = 8 / 13	<i>AIC</i> = 128 / 96 <i>PRR</i> = 0 / 64 <i>SSE</i> = 903 / 27 <i>MSE</i> = 36 / 13
Delayed S-shaped Model	<i>AIC</i> = 279 / 74 <i>PRR</i> = 305 / 94 <i>SSE</i> = 8 / 6627e + 03 <i>MSE</i> = 2296	<i>AIC</i> = 132 / 33 <i>PRR</i> = 6 / 29 <i>SSE</i> = 741 / 74 <i>MSE</i> = 61 / 81	<i>AIC</i> = 78 / 04 <i>PRR</i> = 22 / 22 <i>SSE</i> = 33 / 88 <i>MSE</i> = 1 / 61	<i>AIC</i> = 203 / 74 <i>PRR</i> = 28 / 51 <i>SSE</i> = 4 / 2179e + 03 <i>MS</i> = 168 / 71

According to the results of Table 4, it can be seen that the proposed model has a good fitness on mentioned datasets and works better than the exponential model and delayed S-shaped model.

7. CONCLUSION

Software reliability growth models can be used to determine software performance and control the testing process of software.

Based on these models, reliability is estimated in quantitative methods. Some measurements such as number of initial faults, failure intensity, software reliability in a specified period of time and mean time between failures can be determined by using SRGMs.

By now, various models have been developed by researchers based on software testing conditions.

New software reliability model proposed in this paper, categorizes software faults into simple, independent complex and dependent complex. The model is also affected by imperfect debugging and time delay factor in complex faults removal modelling.

By considering new assumptions more realistic model proposed, which considers both complexity and dependency of faults in its fault removal modelling. Imperfect debugging and time delay factor in removing complex faults are two other important assumptions in new model. So by making this model more closer to real software conditions it can estimate software reliability more accurate than compared basic models.

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¹Prediction Ratio Risk

²Sum of Squared Errors

³Mean Squared Errors

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